

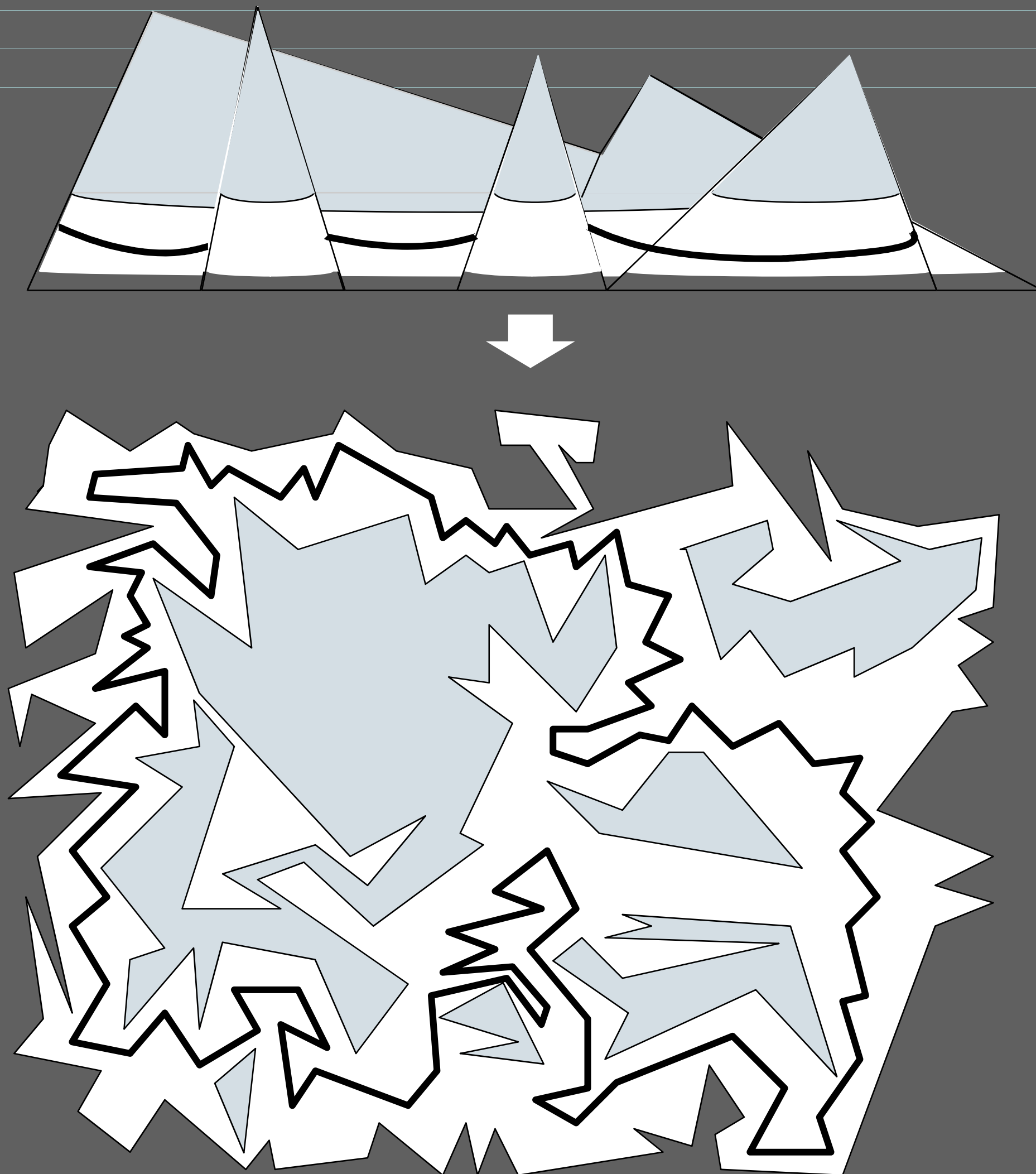
Polygonal Line Simplification

Motivation

Simplification of geometric objects is important in e.g. computer graphics, image processing and geographic information systems (GIS), since simplification both reduces the amount of storage needed and makes the objects easier to assess for the human viewer.

Terrain contour line simplification

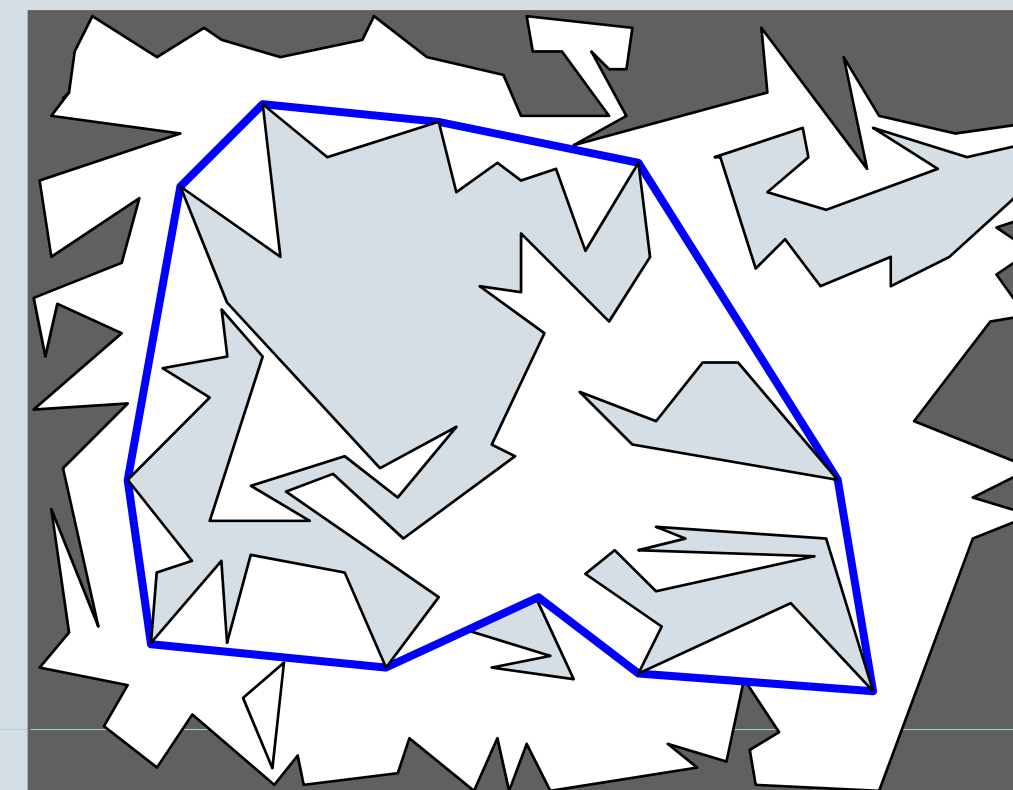
Contour lines from detailed terrain data often need to be simplified. The contours are often very large and I/O-efficient algorithms are needed. A contour line is a polygonal line without self intersections (of size M). Neighboring contour lines form a polygon (of size N) with inner contours as holes. When the polygonal line is simplified, neither self intersections nor intersections with the polygons may be introduced.



Euclidean Shortes Path

Euclidean shortest path (ESP): Minimizing the length of the line.

Can be solved by decomposing the polygon and tracing the line through the decomposition.

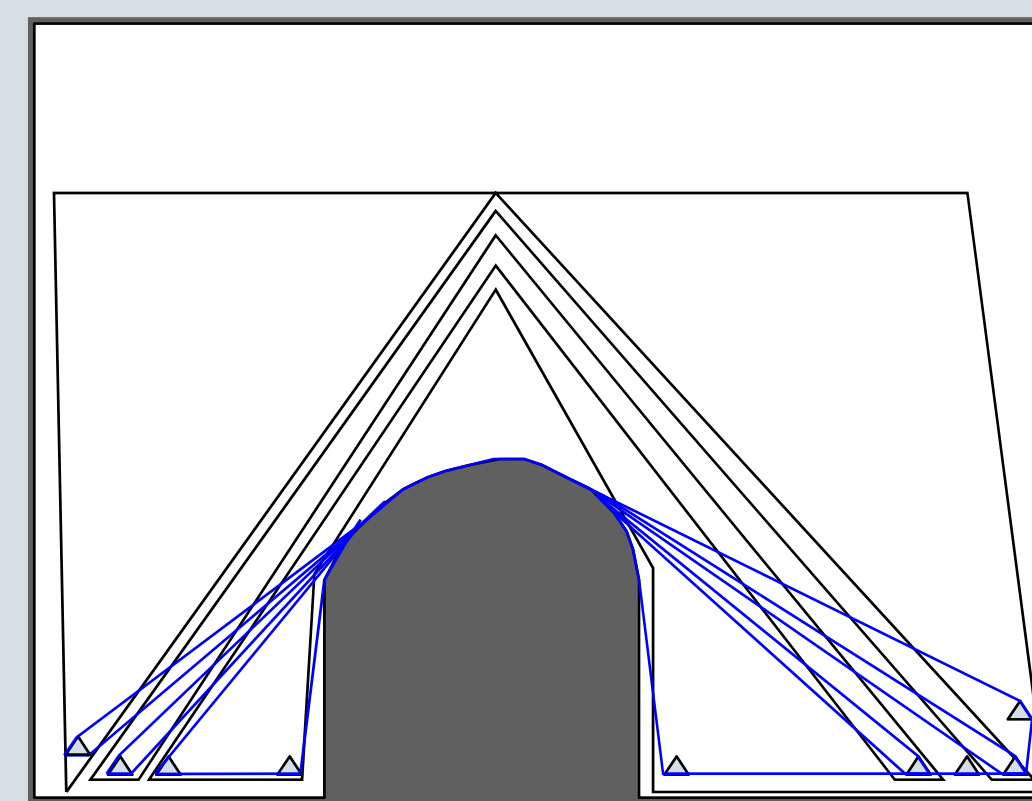


ESP algorithms

Using a geodesic triangulation and a spanning tree [1], ESP takes $O(M \log(N)\sqrt{N} + |ESP|)$ in internal memory.

We have developed an optimal $O(\text{sort}(N))$ I/O-efficient algorithm when there are no holes.

Worst case ESP

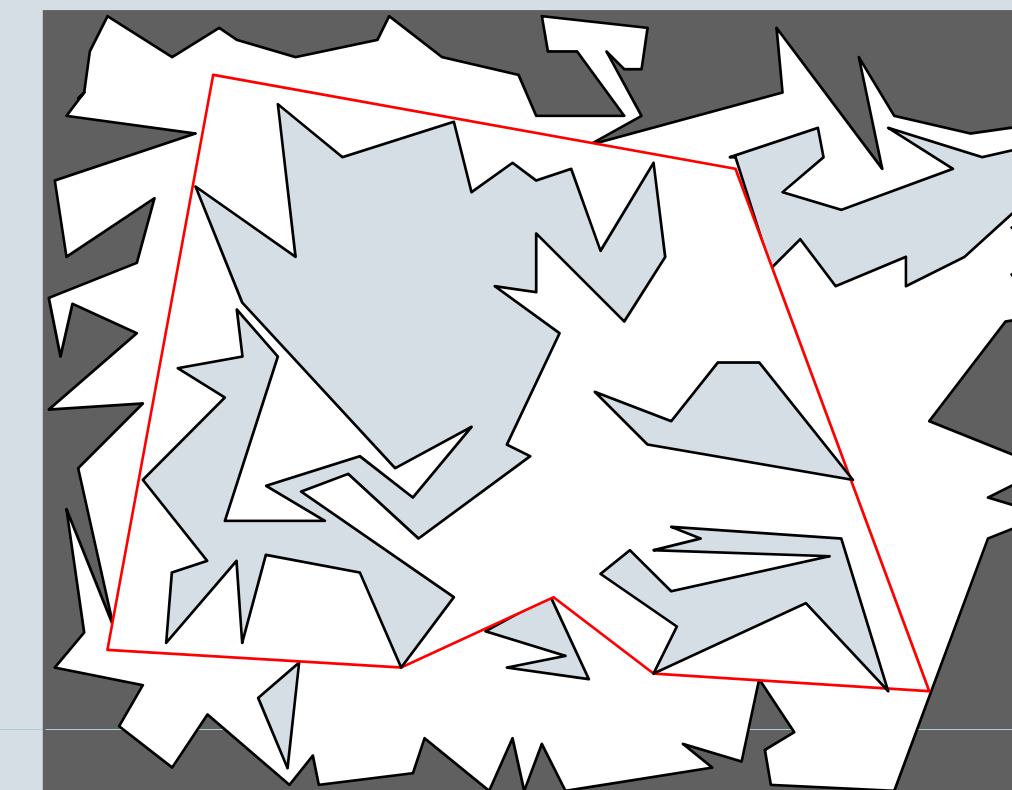


$|ESP|$ can be anything from $\Theta(1)$ to $\Theta(MN)$.

Minimum Link Path

Minimum link path (MLP): Minimizing the number of segments.

Hershberger et al. [2] explained how to extend the ESP algorithm to an MLP algorithm.

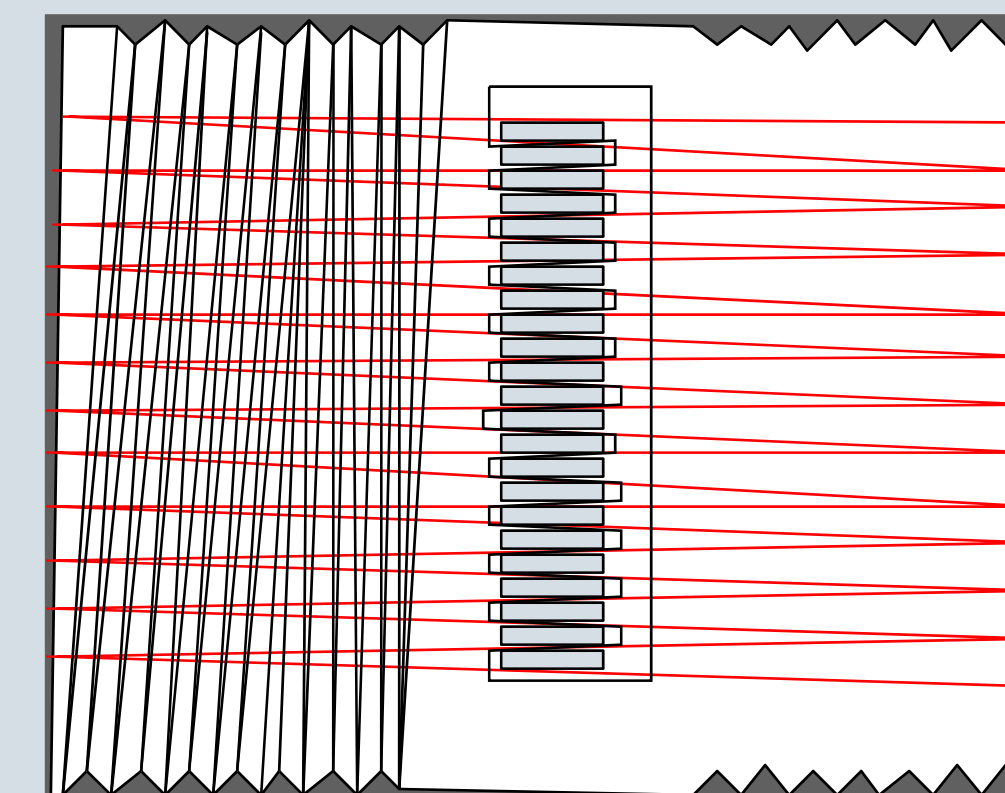


MLP algorithms

By reusing the ESP triangulation, it takes an additional $O(M \log(N)\sqrt{N})$ to find an MLP.

Our I/O efficient algorithm can be extended similarly.

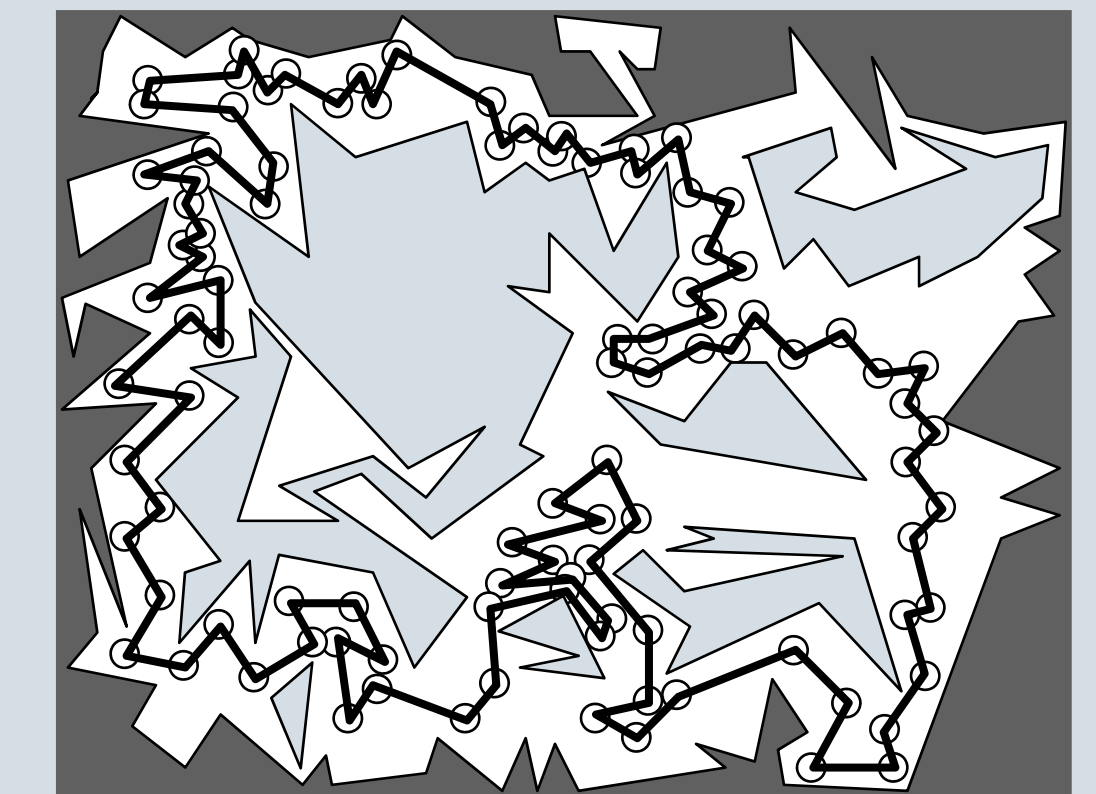
Worst case MLP



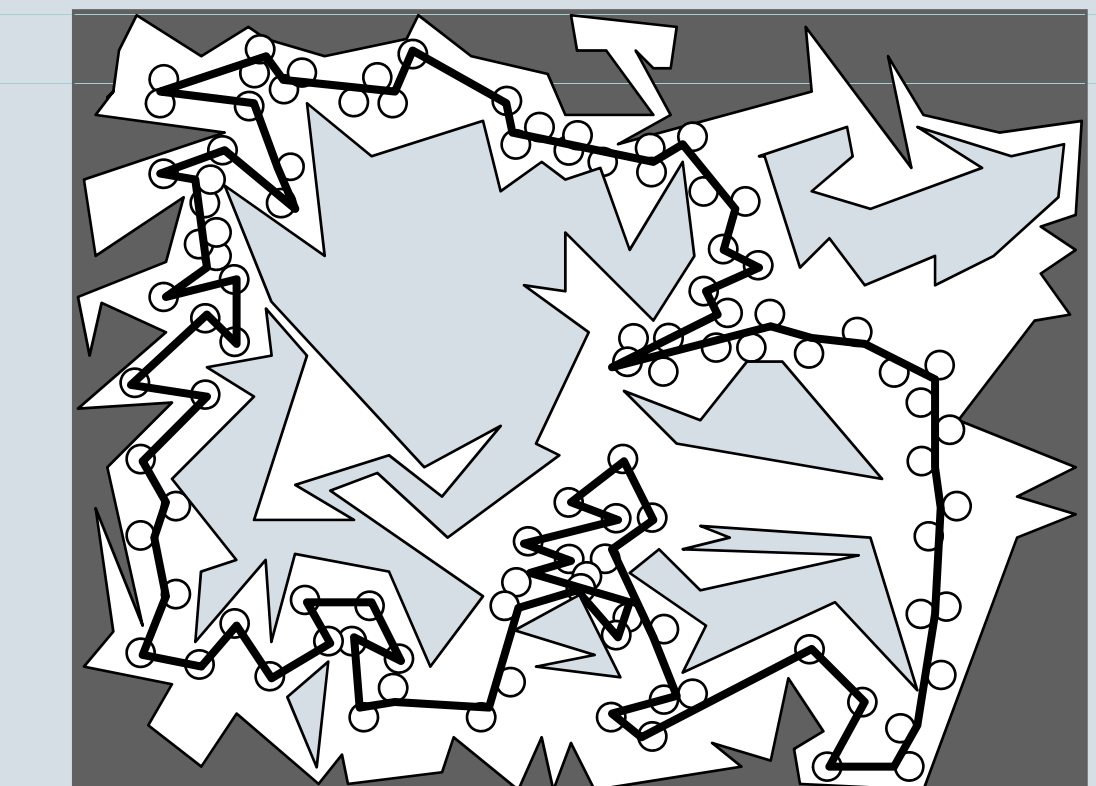
MLP might intersect a lot of triangles while the original path does not (some triangulation are shown).

Heuristics

A simple and fast heuristic might lead to good results in practice.



Suppose discs are drawn around each point, restricting the simplified line to intersect them.



Introducing an additional constraint of each line intersecting at most 10 discs simplifies the algorithm even further.

We plan on experimenting with such heuristics.

References

- [1] Chazelle, Edelsbrunner, Grigni, Guibas, Hershberger, Sharir and Snoeyink. Ray Shooting in Polygons using Geodesic Triangulations, *Algorithmica*, 1994.
- [2] Hershberger and Snoeyink. Computing Minimum Link Paths of a Given Homotopy Class, *WADS*, 1991.